Effect of Inlet and Outlet Flow Conditions on Natural Gas Parameters in Supersonic Separation Process

Yan Yang¹, Chuang Wen¹*, Shuli Wang¹, Yuqing Feng²

1 Jiangsu Key Laboratory of Oil-Gas Storage and Transportation Technology, Changzhou University, Changzhou, Jiangsu Province, China, 2 Computational Informatics, Commonwealth Scientific and Industrial Research Organization, Melbourne, The State of Victoria, Australia

Abstract

A supersonic separator has been introduced to remove water vapour from natural gas. The mechanisms of the upstream and downstream influences are not well understood for various flow conditions from the wellhead and the back pipelines. We used a computational model to investigate the effect of the inlet and outlet flow conditions on the supersonic separation process. We found that the shock wave was sensitive to the inlet or back pressure compared to the inlet temperature. The shock position shifted forward with a higher inlet or back pressure. It indicated that an increasing inlet pressure declined the pressure recovery capacity. Furthermore, the shock wave moved out of the diffuser when the ratio of the back pressure to the inlet one was greater than 0.75, in which the state of the low pressure and temperature was destroyed, resulting in the re-evaporation of the condensed liquids. Natural gas would be the subsonic flows in the whole supersonic separator, if the mass flow rate was less than the design value, and it could not reach the low pressure and temperature for the condensation and separation of the water vapor. These results suggested a guidance mechanism for natural gas supersonic separation in various flow conditions.

Citation: Yang Y, Wen C, Wang S, Feng Y (2014) Effect of Inlet and Outlet Flow Conditions on Natural Gas Parameters in Supersonic Separation Process. PLoS ONE 9(10): e110313. doi:10.1371/journal.pone.0110313

Editor: Gongnan Xie, Northwestern Polytechnical University, China

Received November 22, 2013; Accepted September 21, 2014; Published October 22, 2014

Copyright: © 2014 Yang et al. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

Funding: This work was supported in part by the National Natural Science Foundation of China (No. 51176015) and Jiangsu Key Laboratory of Oil–Gas Storage and Transportation Technology (No. SCZ1211200004/001). The funders had no role in study design, data collection and analysis, decision to publish, or preparation of the manuscript.

Competing Interests: The authors have declared that no competing interests exist.

* Email: wenchuang2008@gmail.com

Introduction

As the global economy rises, the demand for energy supply is increasing continuously in the last two decades. Natural gas plays a significant strategic role in the energy supply [1]. Natural gas is gaseous mixture, primarily composed of methane, ethane, propane and butane, with some heavier alkanes, carbon dioxide, hydrogen sulfide, nitrogen and a small amount of water vapor [2]. The presence of water vapor in natural gas increases the risk of the formation of gas hydrates with line plugging due to hydrate deposition on the pipe walls, results in corrosion combined with acid gases including carbon dioxide and hydrogen sulfide, and reduces the delivery capacity of the pipelines because of the collection of free water [3]. Consequently, the water vapor must be removed from natural gas early on.

At present, many conventional techniques are employed for the natural gas separation, such as absorption, adsorption, refrigeration, membranes and so on. A supersonic separator, as a novel technique, has been introduced to natural gas processing from the beginning of this century [4–6]. In essence, the supersonic separation technique causes refrigeration like the Joule-Thompson effect and Turbine expansion, both of which induce a low temperature for the condensation of water vapor. The supersonic separator mainly consists of a Laval nozzle, a swirl device and a diffuser.

Malyshkina [7,8] obtained the distribution of gas dynamic parameters through a supersonic separator with a computational method, and a procedure was developed to predict the separation capability of water vapor and higher hydrocarbons from natural gas by using a supersonic separator determined by the initial parameters. Karimi and Abdi [9] studied the flow fields of natural gas in a Laval nozzle of 0.12 m long. But the working fluid was assumed to be a supercritical flow. The geometric construction and flow conditions are quite different from the actual flow states of natural gas in a supersonic separator for dehydration. Jiang et al. [10] employed the corrected Internally Consistent Classical Theory and Gyarmathy theory to modelling the nucleation and droplet growth of natural gas in the supersonic separation process. A supersonic separator was compared to a Joule-Thomson valve with TEG and the results demonstrated the high economic performance and natural gas liquids recovery of a supersonic separator [11]. The generalized radial basis function artificial neural networks were used to optimize the geometry of a supersonic separator [12]. Rajaee Shooshtari and Shahsavand developed a new theoretical approach based on mass transfer rates to calculate the liquid droplet growth in supersonic conditions for binary mixtures [13]. In our preliminary studies, a central body was incorporated in a supersonic separator with a swirling device composed of vanes and an ellipsoid [14]. The effects of swirls on natural gas flow in supersonic separators were computationally simulated with the Reynolds stress model [15]. The particle separation characteristic in a supersonic separator was calculated using the discrete particle method [16].

The mechanisms of the upstream and downstream influences are not well understood for various flow conditions from the wellhead and the back pipelines. The purpose of this study is to





Figure 1. Schematic diagram of a supersonic separator. doi:10.1371/journal.pone.0110313.g001

investigate the effects of the operating parameters on natural gas supersonic separation process, including the back pressure, inlet mass flow rates, inlet pressures and inlet temperatures. The Redlich-Kwong real gas model is employed to calculate the gas thermal properties in high pressure and low temperatures in our simulation.

Governing equations

Natural gas can be accelerated to supersonic velocities with a Laval nozzle in a supersonic separator and, accordingly, low pressure and temperature conditions are achieved for water vapor condensation. The fluid structure of natural gas flows can be described by the conservation equations of mass, momentum and energy. To close the partial differential equations, the Shear Stress Transport (SST) [17] turbulence model was used in our simulation to solve the supersonic gas flows.

The mass equation of gas phase (continuity equation) is described as:

$$\frac{\partial}{\partial x_i}(\rho u_i) = 0 \tag{1}$$

where ρ and u are the gas density and velocity, respectively.

The conservation of momentum for gas phase can be written as follows:

$$\frac{\partial}{\partial x_j}(\rho u_i u_j + p \delta_{ij} - \tau_{ji}) = 0$$
⁽²⁾

where p is the gas pressure; τ_{ij} is the viscous stress; δ_{ij} is the Kronecker delta.

The energy equation for gas phase is expressed as Eq. 3.

$$\frac{\partial}{\partial x_i}(\rho u_j E + u_j p + q_j - u_i \tau_{ij}) = 0$$
(3)

where E is the total energy; q_i is the heat flux; t is the time.

The turbulent kinetic energy and the specific dissipation rate equations in SST model are as follows [17,18]:



Figure 2. Pressure profile for nozzle flow. doi:10.1371/journal.pone.0110313.g002

Table 1. Mole composition of natural gas.

Natural gas composition	Mole fraction (%)
CH ₄	91.36
C ₂ H ₆	3.63
C ₃ H ₈	1.44
i-C ₄ H ₁₀	0.26
n-C ₄ H ₁₀	0.46
i-C ₅ H ₁₂	0.17
n-C ₅ H ₁₂	0.16
H ₂ O	0.03
CO ₂	0.45
N ₂	2.04

doi:10.1371/journal.pone.0110313.t001

$$\frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j} \left(\Gamma_k \frac{\partial k}{\partial x_j} \right) + \bar{\mathbf{G}}_k - Y_k + S_k \tag{4}$$

$$\frac{\partial}{\partial x_j}(\rho \omega u_j) = \frac{\partial}{\partial x_j} \left(\Gamma_{\omega} \frac{\partial \omega}{\partial x_j} \right) + G_{\omega} - Y_{\omega} + D_{\omega} + S_{\omega}$$
(5)

where k is the turbulent kinetic energy, ω is the specific dissipation rate. Γ_k and Γ_{ω} represent the effective diffusivity of k and ω , respectively. \overline{G}_k represents the generation of turbulence kinetic energy due to mean velocity gradients. G_{ω} represents the generation of the specific dissipation rate, ω . Y_k and Y_{ω} represent the dissipation of k and ω due to turbulence. D_{ω} represents the cross-diffusion term. S_k and S_{ω} are user-defined source terms.

An equation of state must be developed to calculate the physical property of fluids in supersonic flows. In this simulation, the Redlich-Kwong real gas equation of state model [19] was employed to predict gas dynamic parameters, described in Eq. (6).

$$p = \frac{RT}{V_m - b} - \frac{a}{\sqrt{T}V_m(V_m + b)} \tag{6}$$

where p is the gas pressure, R is the gas constant, T is temperature, V_m is the molar volume (V/n), a is a constant that corrects for attractive potential of molecules, and b is a constant that corrects for volume.

The constants a and b are different depending on which gas is being analyzed. They can be calculated from the critical point data of the gas:

$$a = \frac{0.4275R^2 T_c^{2.5}}{p_c} \tag{7}$$

$$b = \frac{0.08664RT_c}{p_c} \tag{8}$$

where T_c and p_c are the temperature and pressure at the critical point, respectively.

For the multi-component mixtures, such as natural gas, mixing laws are utilized to calculate the parameters a and b. The Van Der Waals mixing rules [20,21] were applied to obtain the parameters for the mixtures from those pure components. The mathematical expressions of this mixing rule can be written,

$$a = \sum_{i=1}^{n} \sum_{j=1}^{n} x_i x_j \sqrt{a_i a_j} (1 - k_{ij})$$
(9)

$$b = \sum_{i=1}^{n} x_i b_i \tag{10}$$

where x is molar fraction; n is the total number of the gas components; k_{ij} is the binary interaction parameter between components i and j.

Mathematical modelling

Computational domain and boundary conditions

A Laval nozzle is a key part of a supersonic separator to generate supersonic flows for the condensation and separation of natural gas. Thus, the nozzle needs to be designed specifically, as shown in Figure 1. The cubic polynomial equation was employed to calculate the converging contour of the nozzle, as shown in Eq. (11), while the Foelsch's analytical calculation method was used to design the diverging part of the nozzle [22]. This design of the converging part will accelerate the gas flow uniformly to achieve the sound speed in the throat area. The critical cross-section area is 0.0002378 m^2 . The nozzle entrance and exit areas are 0.007854 m^2 and 0.0004460 m^2 , respectively. In addition, a straight tube with the length of 100 mm was connected to the nozzle upstream and diffuser downstream, respectively.

$$\begin{cases} \frac{D - D_{cr}}{D_1 - D_{cr}} = 1 - \frac{1}{X_m^2} \left(\frac{x}{L}\right)^3 & \left(\frac{x}{L} \le X_m\right) \\ \frac{D - D_{cr}}{D_1 - D_{cr}} = \frac{1}{\left(1 - X_m\right)^2} \left(1 - \frac{x}{L}\right)^3 & \left(\frac{x}{L} > X_m\right) \end{cases}$$
(11)

where D_1 , D_{cr} and L are the inlet diameter, the throat diameter and the convergent length, respectively. $X_m = 0.45$. x is the distance between arbitrary cross section and the inlet, and D is the convergent diameter at arbitrary cross section of x.

A structured grid was generated for the supersonic separator while a finer grid scheme in the boundary layer was employed in Laval nozzle and supersonic channel. The grid independence was

	Table 2. Init	ial conditions for back pressure simulation.
--	---------------	--

Cases	Inlet pressure (bar)	Inlet temperature (K)	Back pressure (bar)
1	100	300	85
2	100	300	80
3	100	300	75
4	100	300	62



Figure 3. Effect of back pressure on natural gas dynamic parameters. doi:10.1371/journal.pone.0110313.g003



Mach numbers in supersonic separators

Figure 4. Mach numbers in supersonic separators with various back pressures.

doi:10.1371/journal.pone.0110313.g004

tested before we carried out the simulation. Boundary conditions played a significant role in a numerical simulation. In our case related to a supersonic separator, the pressure boundary conditions were assigned for the inlet and outlet of the supersonic separator, respectively, according to the flow characteristics of the supersonic compressible fluid,. No-slip and adiabatic boundary conditions were specified for the walls. The turbulent kinetic energy and turbulent dissipation rate were employed as the turbulence parameters.

Computational methods

The finite volume methods were used to discretize the partial differential equations of the supersonic gas flows. The pressure based implicit solver was employed to solve the governing equations. The SIMPLE algorithm [23] was applied to couple the velocity field and pressure. The standard pressure scheme was adopted to interpolate the pressure values on the surface of the control volume. The second-order upwind scheme was used for other variables, such as density, momentum, turbulence kinetic energy, turbulence dissipation rate.

Validation

For the validation of our computational methods in supersonic flows, it was validated with Arina's results before we applied it to our designed supersonic separator [24,25]. Figure 2 depicts the pressure profiles in a Laval nozzle with the numerical results and Arina's work. It could be seen that the same flow behavior was obtained and the shock wave position was accurately captured by our simulation method. Therefore, the numerical results agree with Arina's results well. It was demonstrated that our developed model could be used in the prediction of the supersonic flow for natural gas dehydration.

Results and Discussion

Effect of back pressure

The flow characteristics of natural gas were numerically simulated in the supersonic separation process. The multicomponents gas mixture in Baimiao gas well of Zhongyuan Oil Field was selected for the calculation. The composition of natural gas in mole fraction is shown in Table 1.

The incoming flow parameters are fixed when we study the effect of the back pressures on the supersonic separation process. The detailed initial conditions for the back pressure simulation are shown in Table 2. Figure 3 presents the static pressure and static temperature profiles along the flow direction in the conditions of different back pressures. The shock wave position moves into the nozzle from the diffuser with the rise of the back pressure. The shock wave will stay in the diffuser while the back pressure is about less than 75 bar with the inlet pressure of about 100 bar. If the back pressure increases to 80 bar, the shock wave will move into the supersonic channel across the diffuser entrance. The pressure and temperature profiles exhibit several fluctuations close to the shock wave and away from it. This is induced by the interaction between the boundary layer separation and the shock boundary layer.

Figure 4 depicts the contours of gas Mach numbers in the supersonic separators with various back pressures. It clearly shows the obvious differences of the shock wave position with the increasing back pressure. In this simulation case, the shock wave even goes into the nozzle diverging part when the back pressure reaches 85 bar. In this condition, the shock wave will destroy the state of the low pressure and temperature, resulting in the re-evaporation of the condensed liquids to decline the separation efficiency of the supersonic separators.

Effect of inlet mass flow rate

A Laval nozzle is a key part in a supersonic separator, and the critical area at the nozzle throat determines the gas mass flow rate through this device. The detailed initial conditions for inlet mass flow rate simulation are shown in Table 3. Figure 5 describes the gas dynamic parameters with various inlet mass flow rate, namely, including the gas Mach number, the static pressure and static

Table 3. Initial conditions for inlet mass flow rate simulation.

Cases	Inlet mass flow rate (kg/s)	Inlet temperature (K)	Back pressure (bar)
1	1.343	300	85
2	2.687	300	85
3	3.493	300	85
4	3.896	300	85
5	4.000	300	85



 Figure 5. Effect of inlet mass flow rate on natural gas dynamic parameters.

 doi:10.1371/journal.pone.0110313.g005

 PLOS ONE | www.plosone.org
 6



Figure 6. Phase envelope and pressure-temperature relationships with various inlet mass flow rates. doi:10.1371/journal.pone.0110313.g006

temperature. If the mass flow rate is less than the design value, the gas velocity at the nozzle throat is less than the critical value, although the converging part speeds up the gas flows. Because of the Mach number at the throat is less than unity, the gas velocity declines in the diverging part of the Laval nozzle. In this situation, the maximum velocity is obtained at the nozzle throat. That is, natural gas is the subsonic flows in the whole supersonic separator, which cannot reach the low pressure and temperature for the condensation of the water vapor. The gas Mach number rises with the increase of the inlet gas mass flow rate, resulting in the decline of the static pressure and temperature. When the inlet gas flow rate reaches the design value, the choked flow conditions will be achieved. In our simulation cases, the critical flow condition is obtained when the inlet gas mass flow rate is about 4.155 kg/s. In this condition, the natural gas flow continues to expand in the diverging part of the Laval nozzle, and the maximum Mach number is around 1.33.

Figure 6 depicts the phase envelope curve and the pressure– temperature (P-T) profiles with various inlet mass flow rates. We can see that P-T profile doesn't reach the phase envelope curve because of the high pressure and temperature in the supersonic separator, when the inlet gas mass flow rate is smaller than the design value. Therefore, the water vapor can hardly be removed from natural gas when the inlet mass flow rate is less than the designed rate.

Effect of inlet pressure

The inlet temperature is fixed and the back pressure is set to be the 85% of the inlet one, when we studied the effect of the inlet pressures on the gas dynamic parameters. The detailed initial conditions for inlet pressure simulation are shown in Table 4. The gas mass flow rate in a supersonic separator increases with the rises of the inlet pressure. It indicates that the processing capacity of a supersonic separator can be improved by increasing the inlet pressure in natural gas processing. Figure 7 presents the gas static

Tab	le 4.	Initial	conditions	for	inlet	pressure	simu	lation.
-----	-------	---------	------------	-----	-------	----------	------	---------

Cases	Inlet pressure (bar)	Inlet temperature (K)	Back pressure (bar)
1	50	300	42.5
2	100	300	85
3	200	300	170
4	300	300	255



Figure 7. Effect of inlet pressure on natural gas dynamic parameters. doi:10.1371/journal.pone.0110313.g007

pressure and temperature profiles along the designed supersonic separator. The shock wave position shifts forward to the nozzle with a higher inlet pressure. For example, the shock position stayed at z = 0.370 m at an inlet pressure of about 50 bar. However, the shock location goes to the upstream of the nozzle divergent part, at z = 0.263 m, when the inlet increases to 300 bar. That is, the shock wave position shifts forward by a distance of

about 97 mm. This numerical simulation indicates that the pressure recovery capacity of the supersonic separator will decline in a higher inlet pressure.

Figure 8 depicts the phase envelope curve and the pressure– temperature (P-T) profiles with various inlet pressures. The P-T profile goes into the gas-liquid two phase zone, although the inlet pressure is changed, when the inlet pressure is lower than 100 Bar.



Figure 8. Phase envelope and pressure-temperature relationships with various inlet pressures. doi:10.1371/journal.pone.0110313.g008

In these conditions the static pressure and temperature is low enough for the condensation of the water vapor in natural gas. But if the inlet pressure exceeds 200 bar, the natural gas flow will present a supercritical fluid in the supersonic separator, which is not suitable for the gas dehydration. Therefore, we suggest that the maximum inlet pressure should be around 100 bar for natural gas dehydration using a supersonic separator.

Effect of inlet temperature

The inlet and back pressure are fixed to study the influence of the inlet temperature. The detailed initial conditions for inlet temperature simulation are shown in Table 5. The gas mass flow rate decreases with the rise of the inlet temperature in the supersonic separator. It indicates that the processing capacity of a supersonic separator can be improved by decreasing the inlet temperature in natural gas processing. It can be seen in Figure 9 that the shock position moves backward from nozzle to diffuser with the increase of the inlet temperature. However, the shock position moves just by a distance of about 5 mm with the increase of the inlet temperature from 10° C to 70° C, which is the normal temperature in natural gas processing. Hence, we can neglect the effect of the inlet temperature on the shock wave position in the supersonic separator. Figure 10 shows that the P-T profile goes further into the gas-liquid two phase zone with the decline of the inlet temperature. This is because the lower inlet temperature will cause a lower static temperature in the Laval nozzle, when the pressure ratio is fixed in the supersonic separator.

Conclusion

The gas dynamic parameters in a supersonic separator were simulated using the Shear Stress Transport (SST) turbulence model and Redlich–Kwong real gas model. The effect of the inlet and outlet flow conditions on the gas dynamic parameters was analyzed in the supersonic separation process, especially on the shock wave position. The gas flow cannot be choked in the supersonic separator, when the inlet mass flow rate is less than the designed one. It results in a high pressure and temperature inside the device and the water vapor cannot be removed from natural gas. The shock wave position shifts forward to the nozzle with a

Tak	ble	5.	Initial	conditions	for	inlet	temperature	simu	lation
-----	-----	----	---------	------------	-----	-------	-------------	------	--------

Cases	Inlet pressure (bar)	Inlet temperature (K)	Back pressure (bar)
1	100	283	85
2	100	303	85
3	100	323	85
4	100	343	85



Figure 9. Effect of inlet temperature on natural gas dynamic parameters. doi:10.1371/journal.pone.0110313.g009

higher inlet pressure. The effect of the inlet temperature on the shock wave position can be neglected when the inlet temperature increases from 10° C to 70° C. The increasing back pressure induces the shock wave position to move forward from the diffuser

to Laval nozzle. The shock wave moves into the supersonic channel or Laval nozzle when the back pressure is about more than 75 bar with the inlet pressure of about 100 bar. The shock



Figure 10. Phase envelope and pressure-temperature relationships with various inlet temperatures. doi:10.1371/journal.pone.0110313.g010

wave will destroy the state of the low pressure and temperature, resulting in the re-evaporation of the condensed liquids.

Acknowledgments

This work was supported in part by the National Natural Science Foundation of China (No. 51176015) and Jiangsu Key Laboratory of Oil– Gas Storage and Transportation Technology (No. SCZ121120004/001).

References

- Soldo B (2012) Forecasting natural gas consumption. Appl Energy 92: 26–37.
 Economides MJ, Wood DA (2009) The state of natural gas. J Nat Gas Sci Eng 1:
- 2. Economides MJ, wood DA (2009) The state of natural gas. J Wat Gas Sci Eng T 1–13.
- 3. Mokhatab S, Poe WA, Speight JG (2006) Handbook of natural gas transmission and processing, Gulf Professional Publishing, Burlington, MA, USA.
- Okimoto D, Brouwer J (2002) Supersonic gas conditioning. World Oil 223: 89– 91.
- Alferov VI, Baguiro LA, Dmitriev L, Feygin V, Imaev S, et al. (2005) Supersonic nozzle efficiently separates natural gas components. Oil Gas J 103: 53–58.
- Wen C, Cao X, Yang Y, Zhang J (2011) Swirling effects on the performance of supersonic separators for natural gas separation. Chem Eng Technol 34(9): 1575–1580.
- Malyshkina MM (2008) The structure of gas dynamic flow in a supersonic separator of natural gas. High Temperature 46: 69–76.
- Malyshkina MM (2010) The procedure for investigation of the efficiency of purification of natural gases in a supersonic separator. High Temperature 48: 244–250.
- Karimi A, Abdi MA (2009) Selective dehydration of high-pressure natural gas using supersonic nozzles. Chem Eng Process 48: 560–568.
- Jiang D, Eri Q, Wang C, Tang L (2011) A fast and efficient numericalsimulation method for suprsonic gas processing. SPE projects, facilities & construction 6(2): 58–64.
- Machado PB, Monteiro JGM, Medeiros JL, Epsom HD, Araujo OQF (2012) Supersonic separation in onshore natural gas dew point plant. J Nat Gas Sci Eng 6: 43–49.
- Mahmoodzadeh Vaziri B, Shahsavand A (2013) Analysis of supersonic separators geometry using generalized radial basis function (GRBF) artificial neural networks. J Nat Gas Sci Eng 13: 30–41.

Author Contributions

Conceived and designed the experiments: CW YY. Performed the experiments: CW YY. Analyzed the data: CW YY. Contributed reagents/materials/analysis tools: CW YY. Wrote the paper: CW YY. Revised the manuscript: CW YY SW YF.

- Rajaee Shooshtari SH, Shahsavand A (2013) Reliable prediction of condensation rates for purification of natural gas via supersonic separators. Sep Purif Technol 116: 458–470.
- Wen C, Cao X, Yang Y (2011) Swirling flow of natural gas in supersonic separators. Chem Eng Process 50(7): 644–649.
- Wen C, Cao X, Yang Y, Li W (2012) Numerical simulation of natural gas flows in diffusers for supersonic separators. Energy 37: 195–200.
- Wen C, Cao X, Yang Y, Zhang J (2012) Evaluation of natural gas dehydration in supersonic swirling separators applying the discrete particle method. Adv Powder Technol 23: 228–233.
- Menter FR (1994) Two-equation eddy-viscosity turbulence models for engineering applications. AIAA Journal 32(8): 1598–1605.
- 18. ANSYS Fluent User Manual, 2011, ANSYS INC.
- Kwak TY, Mansoori GA (1986) Van der waals mixing rules for cubic equations of state. applications for supercritical fluid extraction modeling, Chem Eng Sci 41: 1303–1309.
- 20. Benmekki EH, Kwak TY, Mansoori GA (1987) Supercritical fluids, American Chemical Society, Washington.
- Redlich O, Kwong JNS (1949) On the thermodynamics of solutions. V. an equation of state. fugacities of gaseous solutions. Chem Rev 44: 233–244.
- Foelsch K (1949) The analytical design of an axially symmetric Laval nozzle for a parallel and uniform jet. J Aero Sci 16: 161–166.
- Patankar SV, Spalding DB (1972) A calculation procedure for heat, mass and momentum transfer in three-dimensional parabolic flows. Int J Heat Mass Transfer 1: 1787–1806.
- Yang Y, Wen C, Wang S, Feng Y (2014) Theoretical and numerical analysis on pressure recovery of supersonic separators for natural gas dehydration. Appl Energy 132: 248–253
- Arina R (2004) Numerical simulation of near-critical fluids. Appl Numer Math 51: 409–426.